## Formal Languages and Automata Theory SS2020

Exam, Variant 1
June 17th, 2020
Time Limit: 60 Minutes

This exam contains 4 questions. Total of points is 10 .
Grade Table (for teacher use only)

| Question | Points | Score |
| :---: | :---: | :---: |
| 1 | 1 |  |
| 2 | 3 |  |
| 3 | 4 |  |
| 4 | 2 |  |
| Total: | 10 |  |

## Remarks:

- All subjects are mandatory.
- All the results must be accompanied with detailed solution.
- Carefully read and apply the instructions from the Exam assignment on Google Classroom.

1. (1 point) According to Wikipedia, the current system for car plates in Spain use the nnnn LLL where: nnnn is a sequence number from 0000 to 9999 , LLL is a "counter" comprising three letters, which increments after the sequence number reaches 9999. The consonants B, C, D, F, G, H, J, K, L, M, N, P, R, S, T, V, W, X, Y and Z are used for a total of 80 million possible registrations in the system. For example 1234 ABC.
2. (3 points) (a) ( $0.10+0.10$ points) What is an algorithm for DFA minimization doing and what are its benefits?
(b) $(0.10+0.70$ points) Give example of such an algorithm and explain its steps.
(c) (2 points) Minimize the following DFA using the algorithm at (b). Explain all decisions and steps:

|  | 0 | 1 |
| ---: | :--- | :--- |
| $\rightarrow A$ | $B$ | $E$ |
| $B$ | $C$ | $F$ |
| ${ }^{*} C$ | $D$ | $H$ |
| $D$ | $E$ | $H$ |
| $E$ | $F$ | $I$ |
| ${ }^{*} F$ | $G$ | $B$ |
| $G$ | $H$ | $B$ |
| $H$ | $I$ | $C$ |
| ${ }^{*} I$ | $A$ | $E$ |

3. (4 points) (a) (0.5 points) Write a grammar of type 2 which constructs a palindrome from your first name. Example: From Madalina one gets MadalinaaniladaM.
(b) ( 0.25 points) Formally define a PDA. Explain each notation from the definition.
(c) (0.5 points) What are the similarities and dissimilarities of a PDA and a FA? Use the definitions of the two automata in this comparison.
(d) (1.25 point) Construct a PDA which accepts the palindrome generated by your first name and rejects any other string.
(e) (1.5 point) How does the PDA work on the accepted string? Give 10 instantaneous descriptions and explain the type of acceptance.
4. (2 points) Let $\Sigma=\{a, b, \ldots, z\}$ and $L$ the language of your first and last name.
(a) (0.2 points) Write regular expressions for the first, respectively, the last name.
(b) (0.8 points) From these regular expressions, construct the corresponding $\varepsilon$-NFA using the Thomson encoding. Apply also the Thomson encoding for constructing the $\varepsilon-$ NFA for $L$.
(c) (1 point)Using the eager construction algorithm, transform the $\varepsilon-$ NF into a DFA.
